## MATH 315, Fall 2024 Assignment 23

Due: Monday, December 9

**1.** For the original Blumstein-Larson Model, find each of the following conditional probabilities in terms of the parameters  $p_A$ ,  $p_I$ .  $p_{R1}$ ,  $p_{R2}$  and  $p_{R3}$ :

- (a) Pr(C | A) = Probability that a person who has just been arrested will commit at least one more crime
- (b)  $Pr(A \mid C)$
- (c)  $Pr(C \mid I)$
- (d) Pr(I | A)

2. We investigated the Blumstein-Larson Model with  $p_{R1} = p_{R2} = p_{R3}$ . Suppose that arrest and imprisonment have an effect on the propensity to commit new crimes so that  $p_{R1} = 2 p_{R2} = 4 p_{R3}$ .

With  $p = p_{R3}$  and  $p_A = p_I = 1/4$ , determine  $Pr(C \mid C)$ ,  $Pr(A \mid A)$  and  $Pr(I \mid I)$ . Compare these recidivism measures by plotting them against p.

3. Assume again that  $p_{R1} = p_{R2} = p_{R3} = p$ .

(a) Under what conditions will Pr(C | C) = Pr(A | A) = Pr(I | I)?

(b) If  $p_A = p_I = 1/4$  and the prison warden reports a recidivism measure of .1, what recidivism rates will be reported by the police officer and the person on the street?

(c) Determine all 3 recidivism measures if

- (1)  $p_A = p_I = 1/2$
- (2)  $p_A = p_I = 1/3$
- (3)  $p_A = 1/3 \text{ and } p_I = 2/3$